

## HIGH SCHOOL TECHNICAL MATHEMATICS

### Mathematical Practices

The Standards for Mathematical Practice are essential in the extension of mathematical thinking. Students develop these habits of mind through specific, intentional experiences of writing, reading, talking, and reasoning that connect mathematics to their daily lives and career situations. Even though all of the Standards are important for all quality math courses, the following are highlighted in a technical mathematics course:

- Construct viable arguments and critique the reasoning of others (MP.3)
- Modeling with mathematics (MP.4)
- Attend to precision (MP.6)
- Look for and make use of structure (MP.7)
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**In number and quantity, students should recognize that much of mathematics is concerned with understanding quantities and their relationships. They should pick appropriate units for quantities being modeled, using them as a guide to understand a situation, and be attentive to the level of accuracy that is reported in a solution.**

Fluency 1: Number, Quantity and Measurement		
Standards	Strands	Goals and Performance Objectives
HSN-Q.A.1	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture Probability & Distributions Art & Mathematics	Use units as a way to understand problems and to guide the solution of multi-step problems: choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.
HSN-Q.A.2	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture Probability & Distributions Art & Mathematics	Define appropriate quantities for the purpose of descriptive modeling.

HSN-Q.A.3	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture Probability & Distributions Art & Mathematics	Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.
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**In Algebra and Functions, students should use the understanding of the structure of an algebraic expression, equation, or inequality and the properties to solve problems in a range of situations related to their career pathways. Students should understand the mathematics involved and develop fluency in solving career-based problems.**

Standard 2: Algebra		
Standards	Strand	Goals and Performance Objectives
HSA.CED.3	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture	Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
HSA.SSE.3	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture Probability & Distributions	Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression
HSA.CED.2	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture	Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales
HSA.REI.11	Personal Finance & Banking Optimization Issues Medicine & Physical Science	Explain why the x-coordinates of the points where the graphs of the equations $y=f(x)$ and $y = g(x)$ intersect are the solutions of the equations $f(x) = g(x)$ ; find the solutions approximately, using technology to graph the functions, make

	Business & Agriculture	tables of values, or find successive approximations.
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Standard 3: Functions		
Standards	Strand	Goals and Performance Objectives
HSF-F.4	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture	For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts, intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
HSF-IF.5	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture	Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
HSF-IF.6	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture	Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
HSF-IF.7	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture	Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
HSF-BF.1	Personal Finance & Banking Optimization Issues Medicine & Physical Science Business & Agriculture	Write a function that describes a relationship between two quantities.
HSF-BF.3	Personal Finance & Banking Optimization Issues Medicine & Physical Science	Identify the effect on the graph of replacing $f(x)$ by $f(x)+k$ , $k f(x)$ , $f(kx)$ , and $f(x-k)$ for specific values of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and

	Business & Agriculture	odd functions from their graphs and algebraic expressions for them.
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**Geometric visualization is a critical tool in analyzing and solving problems. Students should experience the power found in using geometric understanding as a problem-solving tool. Students should create geometric models and use physical and computational construction tools to solve career-related problems.**

Standard 4: Geometry		
Standards	Strand	Goals and Performance Objectives
HSG.SRT.8	Business & Agriculture Arts & Mathematics	Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.
HSG.CO.2	Business & Agriculture Arts & Mathematics	Represent transformations in the plane using transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformation that preserve distance and angle to those that do not (e.g. translation versus horizontal stretch)
H1SG.GMD.1	Business & Agriculture Arts & Mathematics	Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone.
HSG.C.5	Business & Agriculture Arts & Mathematics	Derive using similarity the fact that the length of an arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of the sector.
HSG.MG.1	Business & Agriculture Arts & Mathematics	Use geometric shapes, their measures, and their proportions to describe objects (e.g. modeling a tree trunk or a human torso as a cylinder)

**Students should be able to create a visual representation of a data set that is useful in understanding or solving a problem.**

Standard 5: Statistics and Probability		
Standards	Strand	Goals and Performance Objectives
HSS.ID.7	Personal Finance & Banking Optimization Issues	Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data
HSS.ID.8	Medicine & Physical Science Optimization Issues	Compute (using technology) and interpret the correlation coefficient of a linear fit
HSS.MD.6	Probability & Distributions	Use probabilities to make fair decisions (e.g. drawing by lots, using a random number generator)

### **Mathematical Modeling**

Seeing mathematics as a tool to model real-world situations should be an underlying perspective in everything students do, including writing algebraic expressions, creating functions, creating geometric models and understanding statistical relationships. This will help students appreciate the importance of mathematics in their career fields and in daily life.

Strands and Possible Projects for 2021-2022 School Year

<p><b>Personal Finance &amp; Banking</b>                      Checkbook                      Checking/Savings/Money Markets/CDs                      Personal Loans                      Subsidized/Unsubsidized Student Loans                      Car Loans &amp; multi-criteria decision making                      Mortgages</p>	<p><b>Business &amp; Agriculture</b>                      Owning a Franchise                      Starting a Business                      Running a Farm/Ranch                      Apple Orchard (patterns w/numbers)                      Well Issues                      Skeeter growth (exponential work)</p>	<p><b>Probability &amp; Distributions</b>                      Queuing                      Gerrymandering                      Sabermetrics                      absenteeism/graduation rates                      Failure rates/quality control                      Carnival Games using area probability</p>
<p><b>Optimization Issues</b>                      Linear programming                      Optimal Locations                      Gasoline blending                      House flipping                      College admittance                      Queuing                      Circuits (Hamiltonian)</p>	<p><b>Art &amp; Mathematics</b>                      Tessellations (heartcubed for Vday)                      Golden Ratio                      Kites in squares  <a href="https://nrich.maths.org/8301">https://nrich.maths.org/8301</a>                      Parent graphs coloring page                      Ratios in Mullets  <a href="http://mrvaudrey.com/2012/05/03/the-only-lesson-theyll-remember/">http://mrvaudrey.com/2012/05/03/the-only-lesson-theyll-remember/</a></p>	<p><b>Medicine &amp; Physical Science</b>                      Sinusoidal Modeling (daylight hours)                      Quadratic Modeling (CBL readers)                      Linear Regression Modeling                      Genetics mapping                      Barbie Bungee  <a href="https://www.nctm.org/Classroom-Resources/Illuminations/Lessons/Barbie-Bungee/">https://www.nctm.org/Classroom-Resources/Illuminations/Lessons/Barbie-Bungee/</a></p>

Resources:

<https://mathmontana.org/>

AMP - Applied Mathematics Practices Textbook - T. Edwards & K. Chelst, authors

<https://www.youcubed.org/>

[www.nctm.org/Classroom-Resources/Illuminations/Lessons](http://www.nctm.org/Classroom-Resources/Illuminations/Lessons)